## TFY4245/FY8917 Solid State Physics, Advanced Course Problemset 7



## **Problem 1**

- (a) Prove that a Landau free energy would be unbounded from below if the Taylor-expansion stops at an odd-order term.
- (b) Consider a Landau free energy including quadratic, cubic, and quartic terms, and prove that the cubic term forces the transition to the disordered state to be first-order.

## **Problem 2**

Compute the relative dielectric constant at temperatures above the ferroelectric transition temperature  $T_c$  for a Landau free energy:

$$F = -EP + g_0 + \frac{1}{2}g_2P^2 + \frac{1}{4}g_4P^4. \tag{1}$$

In obtaining the equilibrium polarization P, you may neglect the contribution from  $P^4$  compared to  $P^2$ .