

Formulae that may be useful. The meaning of the symbols is assumed to be known.

$$\begin{aligned}\bar{\Psi} &\equiv \Psi^\dagger \gamma^0, \quad \gamma^5 \equiv i\gamma^0 \gamma^1 \gamma^2 \gamma^3, \quad \bar{\Gamma} \equiv \gamma^0 \Gamma^\dagger \gamma^0, \quad \sum_{s=1,2} u^{(s)} \bar{u}^{(s)} = (\gamma^\mu p_\mu + mc), \quad \sum_{s=1,2} v^{(s)} \bar{v}^{(s)} = (\gamma^\mu p_\mu - mc), \\ (\gamma^0)^\dagger &= \gamma^0, \quad (\gamma^0)^2 = 1, \quad \gamma^\nu = \gamma^0 (\gamma^\nu)^\dagger \gamma^0.\end{aligned}\tag{4}$$

Internal lines for some particles: $-ig_{\mu\nu}/q^2, \frac{-i(g_{\mu\nu} - q_\mu q_\nu / M^2 c^2)}{q^2 - M^2 c^2}$.

Some vertex factors for various interactions: $ig_e \gamma^\mu, -\frac{ig_W Z}{2\sqrt{2}} \gamma^\mu (1 - \gamma^5)$.

A Lagrangian describing some type of field: $\mathcal{L} = i\hbar c \bar{\Psi} \gamma^\mu \partial_\mu \Psi - mc^2 \bar{\Psi} \Psi$.

Trace theorems: (below I use the notation $a' \equiv a^\mu \gamma_\mu$)

$$Tr(A + B) = Tr(A) + Tr(B), \quad Tr(\alpha A) = \alpha Tr(A), \quad Tr(ABC) = Tr(CAB) = Tr(BCA).\tag{5}$$

$$g_{\mu\nu} g^{\mu\nu} = 4, \quad \{\gamma^\mu, \gamma^\nu\} = 2g^{\mu\nu}, \quad a' b' + b' a' = 2ab.\tag{6}$$

$$\gamma_\mu \gamma^\mu = 4, \quad \gamma_\mu \gamma^\nu \gamma^\mu = -2\gamma^\nu, \quad \gamma_\mu \gamma^\nu \gamma^\lambda \gamma^\mu = 4g^{\nu\lambda}.\tag{7}$$

$$\gamma_\mu \gamma^\nu \gamma^\lambda \gamma^\sigma \gamma^\mu = -2\gamma^\sigma \gamma^\lambda \gamma^\nu, \quad \gamma_\mu a' \gamma^\mu = -2a'.\tag{8}$$

$$\gamma_\mu a' b' \gamma^\mu = 4ab, \quad \gamma_\mu a' b' c' \gamma^\mu = -2c' b' a'.\tag{9}$$

$$Tr(\gamma^\mu \gamma^\nu) = 4g^{\mu\nu}, \quad Tr(\gamma^\mu \gamma^\nu \gamma^\lambda \gamma^\sigma) = 4(g^{\mu\nu} g^{\lambda\sigma} - g^{\mu\lambda} g^{\nu\sigma} + g^{\mu\sigma} g^{\nu\lambda}).\tag{10}$$

$$Tr(a' b') = 4ab, \quad Tr(a' b' c' d') = 4[(ab)(cd) - (ac)(bd) + (ad)(bc)], \quad \gamma^5 = i\gamma^0 \gamma^1 \gamma^2 \gamma^3.\tag{11}$$

$$Tr(\gamma^5) = 0, \quad Tr(\gamma^5 \gamma^\mu \gamma^\nu) = 0, \quad Tr(\gamma^5 \gamma^\mu \gamma^\nu \gamma^\lambda \gamma^\sigma) = 4i\varepsilon^{\mu\nu\lambda\sigma}.\tag{12}$$

$$Tr(\gamma^5 a' b') = 0, \quad Tr(\gamma^5 a' b' c' d') = 4i\varepsilon^{\mu\nu\lambda\sigma} a_\mu b_\nu c_\lambda d_\sigma,\tag{13}$$

where $\varepsilon^{\mu\nu\lambda\sigma}$ is -1 if $\mu\nu\lambda\sigma$ is an even permutation of 0123, +1 if it is an odd permutation, 0 if any two indices are the same. Finally, the trace over an odd number of γ matrices is zero. One has that $\varepsilon^{\mu\nu\lambda\sigma} \varepsilon_{\mu\nu\kappa\tau} = -2(\delta_\kappa^\lambda \delta_\tau^\sigma - \delta_\tau^\lambda \delta_\kappa^\sigma)$ where δ_ν^μ is the Kronecker delta-function (equal to 1 if $\mu = \nu$, 0 otherwise)